



Momentary liquefaction of porous seabed under vertical seismic action

Weiyun Chen^a, Dongsheng Jeng^b, Guoxing Chen^a, Hongyi Zhao^{c,*},
Rui He^c, Hongmei Gao^a

^a Institute of Geotechnical Engineering, Nanjing Tech University, Nanjing 210009, China

^b Griffith School of Engineering, Griffith University Gold Coast Campus, Queensland, QLD 4222, Australia

^c College of Harbor, Coastal and Offshore Engineering, Hohai University, Nanjing 210098, China

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ABSTRACT

The evaluation of potential liquefaction is an important part in the design of marine structures and offshore installations. However, the liquefaction phenomenon of porous seabed under the action of strong earthquake is traditionally been ignored. This paper aims to explore the momentary liquefaction mechanism of porous seabed through the newly analytical solutions of seabed response induced by vertical seismic excitation. Based on the boundary conditions at the surface and bottom of the seabed, the induced displacements and pore pressure in the sediment are rigorously derived as a function of seawater depth, seabed parameters and seismic characteristics of bedrock. A criterion of earthquake liquefaction in the seabed is developed, employing the concept of induced excess pore pressure. The representative cohesionless marine soils with different properties are selected in the parametric analysis. The results show that the liquefaction of seabed could be influenced by seawater parameters, seabed parameters and earthquake ground motion parameters. The significant finding is that current understanding that the vertical motion effect on soil liquefaction is negligible may not always hold true.

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1. Introduction

Liquefaction is a process that material transforms from initially solid state into liquid state. Theoretical analysis of this phenomenon has for decades been a great challenge in geomechanics, earthquake engineering as well as marine engineering [1–3]. In the marine environment, liquefaction also plays an important role around and beneath offshore structures, as it often occurs in saturated or nearly saturated granular materials, like noncohesive seabed soils. The liquefaction of seabed may lead to destructive consequences, such as floating up of pipelines in the seabed, tilting of caissons and deformation of undersea tunnel. Hence the evaluation for liquefaction behavior of seabed is of practical significance in the design and construction of marine structures and offshore installations.

Massive liquefaction of the seabed happens as a result of pore pressure change and the corresponding degradation of the soil's macroscopic properties. Generally, the pressure change of the water trapped in soil skeleton pore comes from external excitation

such as ocean-waves and earthquake. The issue of ocean-waves induced seabed response and instability has attracted great attention from geotechnical and coastal engineers since 1970s [4–7]. The water waves propagating on the ocean could create significant dynamic wave pressure on the seabed surface and cyclic pore pressure in marine sediments [8]. Owing to the phase lags and damping of the dynamic wave pressure, the excess pore pressure is produced from the difference between the wave pressure on the seabed surface and pore pressure in the sediment. When the value of the excess pore pressure directly exceeds a certain mean level, the vertical effective stress vanishes and the momentary liquefaction may happen in the seabed [9]. Other mechanism is wave-induced residual liquefaction, which is due to the build-up of excess pore pressure caused by the volumetric compaction under cyclic wave loading [10].

On the other hand, apart from the ocean-waves, catastrophic damage to offshore structures has also been recorded in the past earthquakes [11,12]. However, the analytical and numerical investigations on seismic dynamics of porous seabed are still limited to date [13–16]. The behaviors of the loads from ocean-waves and earthquake are both periodic but have notably different characteristics (see Table 1). In general, seismic waves propagate in the form of shear and compressional waves, which depends on the vibrating

* Corresponding author.

E-mail address: hyzhao@hhu.edu.cn (H. Zhao).

Table 1
Comparison between wave-induced and vertical-earthquake induced liquefaction in seabed.

	Ocean-waves	Earthquake
Loading type	Oscillating pressure	Stochastic acceleration
Loading position	Seabed surface	Lower bedrock surface
Drainage condition	Partially drained	Approximately undrained
Duration	Few hours or longer	Few minutes or shorter
Location of liquefaction	Near seabed surface	Near seabed surface
Liquefaction type	Cumulative or instantaneous	Mostly instantaneous

direction of the substrate bedrock. The behavior of external cyclic shearing of saturated soil have been confirmed experimentally by dozens of independent laboratories [17–19]. Most of these tests have simulated the liquefaction triggered by shear waves, revealing that the build-up of excess pore pressure in the response could reduce the effective stresses and subsequently the shearing resistance of the soil skeleton. This mechanism results from the ‘residual’ nature of the excess pore pressure, which accumulates gradually after a certain number of wave cycles. This phenomenon is similar to the residual liquefaction induced by ocean waves, caused by the build-up of the excess pore pressure [10].

The other potential liquefaction induced by compressional waves, however, was rarely regarded in geotechnical earthquake engineering, especially through theoretical analysis. As discussed by Yang [20], the understanding that the effect of vertical motion on liquefaction is negligible may not always hold true and the effect is dependent on the saturation condition. The purpose of this study is to explore the momentary liquefaction mechanism in the marine porous sediment which is subjected to vertical seismic action. A new analytical solution for the induced displacements and pore pressure in the seabed are mathematically obtained based on the poro-elastic theory. The effects of several pertinent parameters on the earthquake-induced distribution of liquefied area are then discussed in detail.

2. Governing equations and general solutions

2.1. Governing equations for the seabed

In this study, the marine sediment is considered as a mixture consisting of solid skeletal frame, liquid phase, and gas phase. Some basic assumptions are introduced to derive the analytical solutions for the phenomenon described, such as:

- the partially saturated sediment is homogeneous and hydraulically isotropic material;
- the seabed is elastic, porous, horizontal and of finite thickness;
- both the soil skeleton and the pore fluids are compressible;
- the soil skeleton generally obeys Hooke’s law, implying linear, reversible and non-retarded mechanical properties;
- the flow in the porous seabed is governed by Darcy’s law.

The governing equations for the dynamic response of porous seabed is developed in this section, following the formulation in Zienkiewicz et al. [21] and Ulker and Rahman [22]. The equilibrium equation for the overall porous medium can be written as

$$\sigma_{ij,j} + \rho g_i - \rho \ddot{u}_i - \rho_f \ddot{w}_i = 0 \tag{1}$$

where σ_{ij} is total stress, g_i is the gravitational acceleration, ρ denotes the total density of porous medium, $\rho = (1 - n)\rho_s + n\rho_f$, ρ_s , ρ_f is the fluid density, u_i represents the displacement of soil

skeleton, \bar{w} is the average pore fluid displacement relative to solid frame and is defined as

$$\bar{w} = n (w_f - u) \tag{2}$$

where w_f is the total displacement of the pore fluid.

The equilibrium of fluid can be written as

$$-p_{,j} + \rho_f g_i - \rho_f \ddot{u}_i - \frac{\rho_f}{n} \ddot{w}_i - \frac{\rho_f g_i}{k_f} \dot{w}_i = 0 \tag{3}$$

where p is the pore fluid pressure, k_f is the hydraulically isotropic permeability of porous seabed.

The mass conservation equation can be expressed as

$$\dot{u}_{i,i} + \dot{w}_{i,i} = -n\beta\dot{p} \tag{4}$$

where β is the compressibility of pore fluid defined as [23,24]

$$\beta = \frac{1}{K_w} + \frac{1 - S_r}{p_{w0}} \tag{5}$$

where K_w is the true bulk modulus of water, S_r is the saturation degree, p_{w0} is the absolute water pressure, i.e., $p_{w0} = \rho_f g d$, d is the water depth.

The constitutive relationship between effective stress σ'_{ij} and pore fluid pressure p can be represented by [21,22]

$$\sigma_{ij} = \sigma'_{ij} - \delta_{ij}p \tag{6}$$

where δ_{ij} is Kronecker delta; Note that total stress σ_{ij} and effective stress σ'_{ij} are considered to be positive; p is pore pressure and tension is taken as a positive in this equation.

The strain ε_{ij} is defined as:

$$\varepsilon_{ij} = \frac{1}{2} (u_{i,j} + u_{j,i}) \tag{7}$$

where $u_{i,j}$ and $u_{j,i}$ denote the derivatives of the solid displacement with respect to spatial coordinates.

The constitutive relations of the skeleton can be defined incrementally in terms of effective stress changes as

$$\Delta\sigma'_{ij} = D_{ijkl}\Delta\varepsilon_{kl} \tag{8}$$

where D_{ijkl} is the tangent coefficient matrix and $\Delta\varepsilon_{kl}$ is the strain change from initial state. In plane strain, the effective stress change can be rewritten as

$$\Delta\sigma'_{ij} = \lambda\Delta\varepsilon_{kk}\delta_{ij} + 2\mu\Delta\varepsilon_{ij} \tag{9}$$

where λ and μ are Lamé’s parameters, $\Delta\varepsilon_{kk}$ is volumetric strain change. μ is also called shear modulus and $\lambda = 2\mu\nu/(1 - 2\nu)$ with the Poisson’s ratio ν .

Herein, a porous sediment layer lying on the bedrock is considered, as depicted in Fig. 1. The depth of upper seawater is d and the thickness of poroelastic seabed is L . The z -direction is measured as positive upwards from the bedrock surface, while x -direction is parallel to the horizontal seabed surface. The steady-state displacement of seismic excitation is specified vertically on the impermeable bedrock surface. Accordingly, the variables \tilde{u} and \tilde{w} are adopted to represent the earthquake-induced soil skeleton displacement and average fluid relative displacement in z -direction, respectively. In this linear elastic system, the Eqs. (1)–(3) in absence of body force can reduce to:

$$\left(\lambda + 2\mu + \frac{1}{n\beta}\right) \frac{\partial^2 \tilde{u}}{\partial z^2} + \frac{1}{n\beta} \frac{\partial^2 \tilde{w}}{\partial z^2} - \rho \frac{\partial^2 \tilde{u}}{\partial t^2} - \rho_f \frac{\partial^2 \tilde{w}}{\partial t^2} = 0 \tag{10}$$

$$\frac{1}{n\beta} \left(\frac{\partial^2 \tilde{u}}{\partial z^2} + \frac{\partial^2 \tilde{w}}{\partial z^2} \right) - \frac{\rho_f g}{k_f} \frac{\partial \tilde{w}}{\partial t} - \rho_f \frac{\partial^2 \tilde{u}}{\partial t^2} - \frac{\rho_f}{n} \frac{\partial^2 \tilde{w}}{\partial t^2} = 0 \tag{11}$$

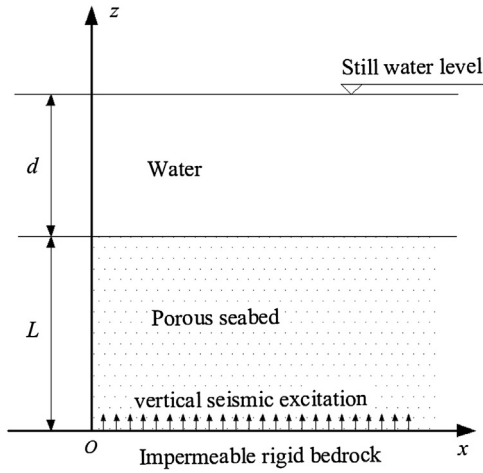


Fig. 1. Schematic diagram of the seismic problem.

Combining Eqs. (10) and (11), the governing equation for the soil skeleton displacement can be expressed as a four-order equation

$$\frac{\partial^4 \tilde{u}}{\partial t^4} + a_1 \frac{\partial^3 \tilde{u}}{\partial t^3} + a_2 \frac{\partial^2 \tilde{u}}{\partial t^2 \partial z^2} + a_3 \frac{\partial \tilde{u}}{\partial t \partial z^2} + a_4 \frac{\partial^2 \tilde{u}}{\partial z^4} = 0 \quad (12)$$

with

$$a_1 = -\frac{n\rho g}{k_f(n\rho_f - \rho)} \quad a_2 = \frac{n\rho + \rho_f[(\lambda + 2\mu)n\beta + 1 - 2n]}{\rho_f n\beta(n\rho_f - \rho)}$$

$$a_3 = \frac{g[(\lambda + 2\mu)n\beta + 1]}{\beta k_f(n\rho_f - \rho)} \quad a_4 = -\frac{\lambda + 2\mu}{\beta \rho_f(n\rho_f - \rho)}$$

2.2. Analytical solutions for response variables

Since the analysis is restricted to a linear periodic response, it is expedient to employ complex variables and then the earthquake-induced displacements are assumed as

$$\begin{Bmatrix} \tilde{u} \\ \tilde{w} \end{Bmatrix} = \begin{Bmatrix} u_0 \\ w_0 \end{Bmatrix} \exp[i(\omega t - zk)] \quad (13)$$

where u_0 and w_0 represent the corresponding amplitudes, i is the root of -1 , t denotes time, ω is the angular frequency, k is a complex number. Then Eq. (12) becomes

$$a_4 k^4 + (a_2 \omega^2 - ia_3 \omega)k^2 + \omega^4 - ia_1 \omega^3 = 0 \quad (14)$$

Four different roots can be solved for Eq. (14) as $\pm k_{p1}$ and $\pm k_{p2}$. In soil dynamics, k_{p1} and k_{p2} represent the wave numbers for the fast and slow compressional waves in the saturated soils [25]. Then, the general analytical solutions for solid displacement \tilde{u} and average relative fluid displacement \tilde{w} can be represented as (for brevity the steady-state factor $\exp(i\omega t)$ is omitted)

$$\tilde{u} = b_1 \exp(-ik_{p1}z) + b_2 \exp(ik_{p1}z) + b_3 \exp(-ik_{p2}z) + b_4 \exp(ik_{p2}z) \quad (15)$$

$$\tilde{w} = b_1 \eta_1 \exp(-ik_{p1}z) + b_2 \eta_2 \exp(ik_{p1}z) + b_3 \eta_3 \exp(-ik_{p2}z) + b_4 \eta_4 \exp(ik_{p2}z) \quad (16)$$

with

$$\eta_1 = \eta_2 = \frac{(\lambda + 2\mu + \frac{1}{n\beta})k_{p1}^2 - \omega^2 \rho}{\omega^2 \rho_f - \frac{1}{n\beta}k_{p1}^2} \quad (17)$$

$$\eta_3 = \eta_4 = \frac{(\lambda + 2\mu + \frac{1}{n\beta})k_{p2}^2 - \omega^2 \rho}{\omega^2 \rho_f - \frac{1}{n\beta}k_{p2}^2} \quad (18)$$

For the homogeneous seabed shown in Fig. 1, the evaluation of coefficients b_j ($j = 1 - 4$) in Eqs. (15)–(16) requires appropriate boundary conditions. Firstly, at seabed surface ($z=L$), the seismically induced pore pressure \tilde{p} equals to the induced dynamic pressure of the overlying seawater \tilde{p}_w , while the induced vertical effective stress $\tilde{\sigma}'_{zz}$ disappears. The continuity of fluid volume should also be considered to describe the induced displacements of pore fluid and upper seawater. Thus, these surface boundary conditions are given as

$$-\tilde{p} = \tilde{p}_w, \quad \tilde{\sigma}'_{zz} = 0, \quad \tilde{w}_u = (1 - n)\tilde{u} + n\tilde{w}_f = \tilde{u} + \tilde{w} \quad \text{at } z = L \quad (19)$$

where \tilde{w}_u is the induced displacement of seawater above the seabed surface. \tilde{w}_f is the induced displacement of pore fluid in the soils. \tilde{p}_w is the dynamic seawater pressure induced by the vibration of seabed, the negative sign is due to the definition that pore pressure is taken as negative in Eq. (6). The dynamic seawater pressure takes the form as [26,27]

$$\tilde{p}_w = \rho_f d \ddot{\tilde{w}}_u \quad (20)$$

Secondly, no vertical relative flow occurs at the horizontal seabed bottom where the vertical displacement excitation is acting at, i.e.,

$$\tilde{u} = u_0 \exp(i\omega t), \quad \tilde{w} = 0 \quad \text{at } z = 0 \quad (21)$$

Enforcing the above boundary conditions at both the seabed surface and bottom, the following matrix form can be obtained

$$[M][b_1, b_2, b_3, b_4]^T = [N] \quad (22)$$

The explicit expressions of the elements m_{ij} of $[M]$ are given as follows

$$m_{11} = m_{12} = m_{13} = m_{14} = 1 \quad (23a)$$

$$m_{21} = \eta_1 \quad m_{22} = \eta_2 \quad m_{23} = \eta_3 \quad m_{24} = \eta_4 \quad (23b)$$

$$m_{31} = -k_{p1} \exp(-ik_{p1}L) \quad (23c)$$

$$m_{32} = k_{p1} \exp(ik_{p1}L)$$

$$m_{33} = -k_{p2} \exp(-ik_{p2}L)$$

$$m_{34} = k_{p2} \exp(ik_{p2}L)$$

$$m_{41} = [n\beta\rho_f d\omega^2 - i(1+\eta_1)k_{p1}] \exp(-ik_{p1}L)$$

$$m_{42} = [n\beta\rho_f d\omega^2 + i(1+\eta_2)k_{p1}] \exp(ik_{p1}L)$$

$$m_{43} = [n\beta\rho_f d\omega^2 - i(1+\eta_3)k_{p2}] \exp(-ik_{p2}L)$$

$$m_{44} = [n\beta\rho_f d\omega^2 + i(1+\eta_4)k_{p2}] \exp(ik_{p2}L) \quad (23d)$$

The elements in $[N]$ are given by

$$n_1 = u_0, \quad n_2 = n_3 = n_4 = 0 \quad (24)$$

Then the undetermined coefficients b_j ($j = 1 - 4$) in Eqs. (15)–(16) can be solved. Based on the constitutive relations, the earthquake-induced pore pressure generated in the seabed can be further expressed as

$$\tilde{p} = \frac{i}{n\beta} \begin{bmatrix} b_1(1 + \eta_1)k_{p1} \exp(-ik_{p1}z) - b_2(1 + \eta_2)k_{p1} \exp(ik_{p1}z) \\ + b_3(1 + \eta_3)k_{p2} \exp(-ik_{p2}z) - b_4(1 + \eta_4)k_{p2} \exp(ik_{p2}z) \end{bmatrix} \quad (25)$$

3. Characteristics of seismic-induced response in porous seabed

Under the load of earthquake, the induced displacements and pore pressure in seabed always play an important role around and beneath the offshore structures such as submarine pipeline and tunnel. Okusa [28] demonstrated that saturation degree was an influential factor in the evaluation of seabed response under the

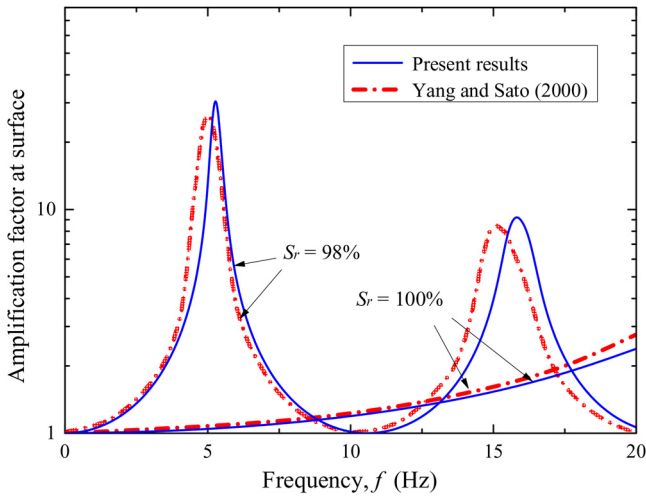


Fig. 2. Effects of frequency on the amplification factor of displacement at seabed surface when the seawater is removed (i.e., $d=0$ m).

action of ocean-waves. Based on the obtained analytical solutions, this section aims to investigate the effects of soil permeability and earthquake frequency on the seismic-induced displacements and pore pressure in the porous seabed with full saturation or partly saturation. To have a basic understanding of the response characteristics, we discuss three types of non-cohesive marine soils which are associated with distinct values of permeability. For example, $k_f=10^{-4}$ m/s is assumed for fine sand, $k_f=10^{-3}$ m/s for medium sand and $k_f=10^{-2}$ m/s for coarse sand [29]. In the following calculation, the density of solid grain $\rho_s=2650$ kg/m³, the density of water $\rho_f=1030$ kg/m³ and the bulk modulus of water $K_w=2.0$ GPa.

First, the motion amplification factor at the seabed surface without seawater (i.e., $d=0$ m) is compared with the previous method [28], as shown in Fig. 2. Here the amplification factor is defined as the ratio of the amplitude of solid displacement at any depth to that at the bottom of seabed. The main parameters of the comparison are: $n=0.37$, $k_f=0.001$ m/s, $\mu=65$ MPa, $L=15$ m, $d=0$ m. It is indicated from Fig. 2 that the present results agree overall with Yang and Sato [30], especially for the fully saturated seabed ($S_r=100\%$) within the common frequency range of undersea earthquake. When the compressibility of solid grains is neglected, the governing equations in Yang and Sato [30] are identical with Eqs. (10) and (11). The discrepancy between the present study and Yang and Sato [30] may come from different derivation process of solutions and the compressibility of grains which is neglected here.

In Figs. 3 and 4, the vertical distribution of maximum amplitudes of earthquake-induced solid displacement $|\tilde{u}|$, relative fluid displacement $|\tilde{w}|$ and pore pressure $|\tilde{p}|$ versus relative soil depth (z/L) is presented. The influence of soil permeability and excitation frequency is respectively illustrated. The solid displacement and relative fluid displacement are non-dimensionalized with respect to the displacement amplitude at the seabed bottom while the pore pressure is normalized by the absolute hydrostatic water pressure at the seabed surface. The situations of both full saturation ($S_r=100\%$) and part saturation ($S_r=99\%$) are considered. It should be noted that the partial saturation of 99% used here is just a research hypothesis that may possibly be found in the real seabed soil [31]. Significant difference is noticed between the seismically induced response in partial and full saturations. It may be related with the fact that the compressibility of pore fluid β drops rapidly when the saturation degree is close to 100%, as depicted in Fig. 5.

In Fig. 3(a), compared with the results of full saturation, the induced solid displacement $|\tilde{u}|$ in the case of incomplete saturation is usually much greater. Thus it should be noted that a saturated

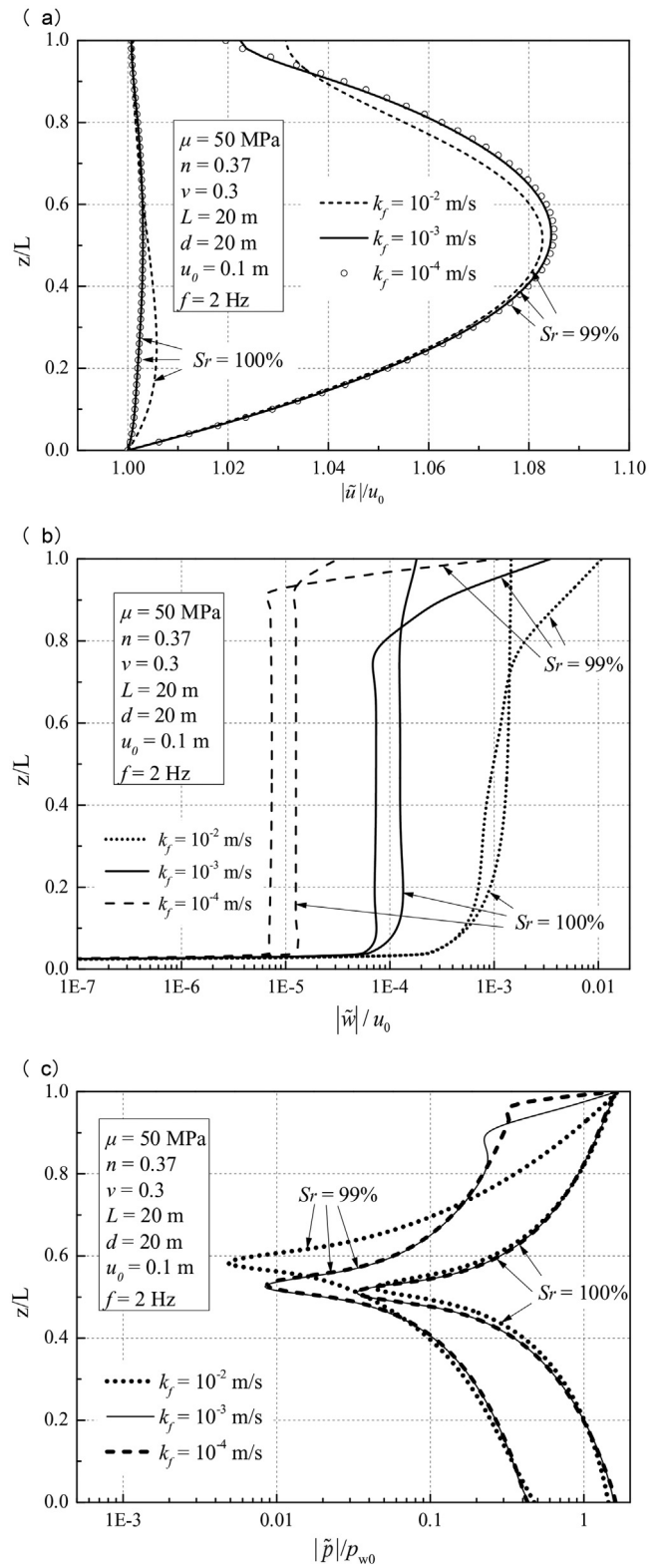


Fig. 3. Vertical distributions of (a) $|\tilde{u}|/u_0$, (b) $|\tilde{w}|/u_0$, and (c) $|\tilde{p}|/p_{w0}$ versus the relative soil depth (z/L) for various soil permeabilities.

model will always underestimate the motion amplification in the seabed. Compared with relative fluid displacement $|\tilde{w}|$ in Fig. 3(b), the induced solid displacement $|\tilde{u}|$ in Fig. 3(a) is less sensitive to the change of soil permeability in both the cases of full saturation and part saturation. This finding is due to the fact that the motion of fluid flowing in the pore of seabed is closely related to

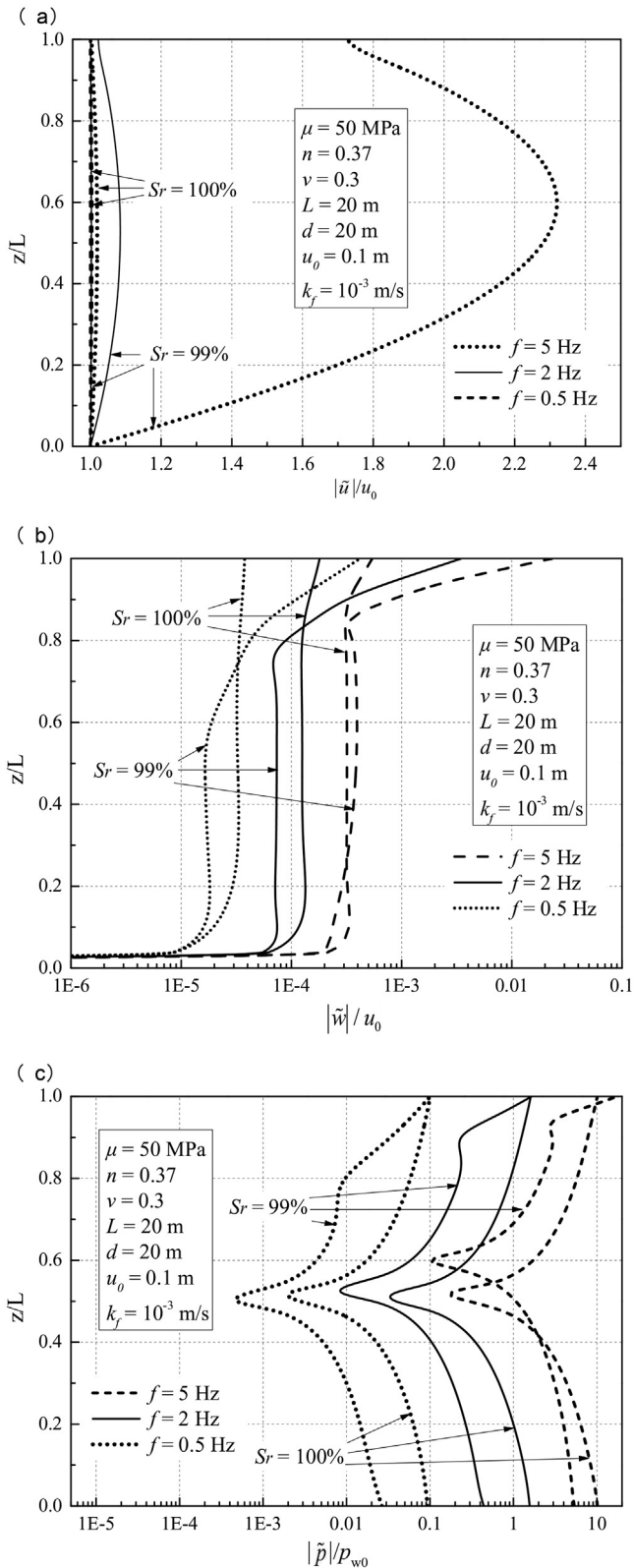


Fig. 4. Vertical distributions of (a) $|\tilde{u}|/u_0$, (b) $|\tilde{w}|/u_0$, and (c) $|\tilde{p}|/p_{w0}$ versus the relative soil depth (z/L) for various excitation frequencies.

the permeability of the soil. Since the higher the permeability is, the resistance between the solid skeleton and pore fluid is weaker, the relative fluid flow becomes larger. As illustrated in Fig. 3(b), the induced relative fluid displacement increases with the increasing permeability. Moreover, the fluid displacement grows rapidly near the seabed surface while drop quickly near the seabed bottom. This

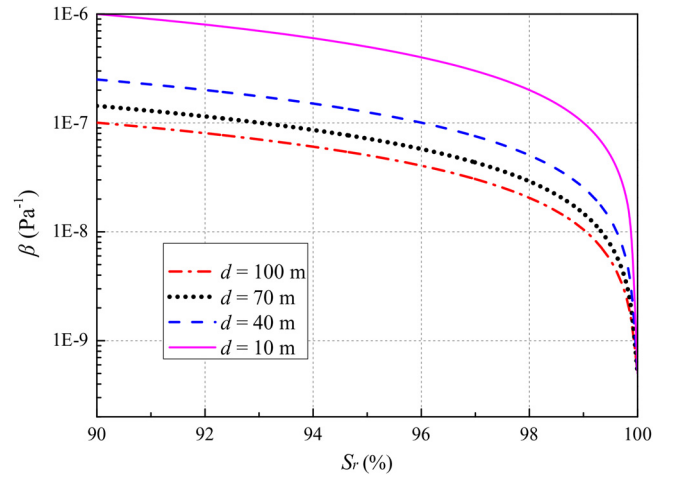


Fig. 5. Variation of the compressibility of pore fluid β with saturation degree S_r for different water depths.

can be explained by the open-pore boundary between seawater and seabed surface and impermeability of seabed bottom. The increasing trend of $|\tilde{w}|$ near the surface of incompletely saturated seabed is shown to be more obvious and this trend also increases with the decrease of permeability. As shown in Fig. 3(c), greater pore pressure is generated in the nearly saturated case. When the soil permeability is relatively low, such as $k_f \leq 10^{-3}$ m/s, the influence of permeability on the induced displacement and pore pressure in most part of the seabed is insignificant.

In Fig. 4(a), the vertical displacement changes more significant from the seabed bottom to its upper surface with the increasing of frequency. This finding is certainly reasonable from an intuitive point of view, since the case of sufficiently low frequency will approach to the quasi-static state and the whole seabed will have the same displacement. Similarly, as depicted in Fig. 4(b), the induced relative fluid displacement increases with the increasing frequency. In most depth of seabed, greater pore pressure is induced under the earthquake of higher frequency when the frequency is higher than 2 Hz, as shown in Fig. 4(c).

4. Momentary liquefaction of seabed

4.1. Criteria of momentary liquefaction

To apply an analysis on seismic-induced liquefaction in porous seabed, Fig. 6 shows the schematic drawings of vertical distribution of the (pore) water pressure and effective vertical stress. In Fig. 6(a), the solid lines *a* and *b* indicate vertical distributions for the maximum and minimum (pore) water pressure beneath the downward and upward earthquake peaks, respectively. In Fig. 6(b), lines *a* and *b* represent the corresponding vertical effective stresses in the seabed under opposite earthquake peaks. In general, the excess pore pressure, also called the excess hydrostatic pressure, is defined as the excess component of pressure beyond the hydrostatic pressure. Because the induced dynamic seawater pressure on the seabed surface varies so quickly that it is not thoroughly propagated into the deposit. Thus the excess pore pressure $p_e(z, t)$, as shown in Fig. 6(a), is represented by the difference between the water pressure change imposed on the seabed surface and the induced pore pressure change from the initial hydrostatic state [9]:

$$p_e(z, t) = \tilde{p}(z, t) - \tilde{p}(L, t) \quad (26)$$

where $\tilde{p}(z, t)$ denotes the seismically induced pressure at a certain depth in the seabed, i.e., the change from hydrostatic pressure to lines *a* and *b* in Fig. 6(a). $\tilde{p}(L, t)$ represents the hydrostatic pres-

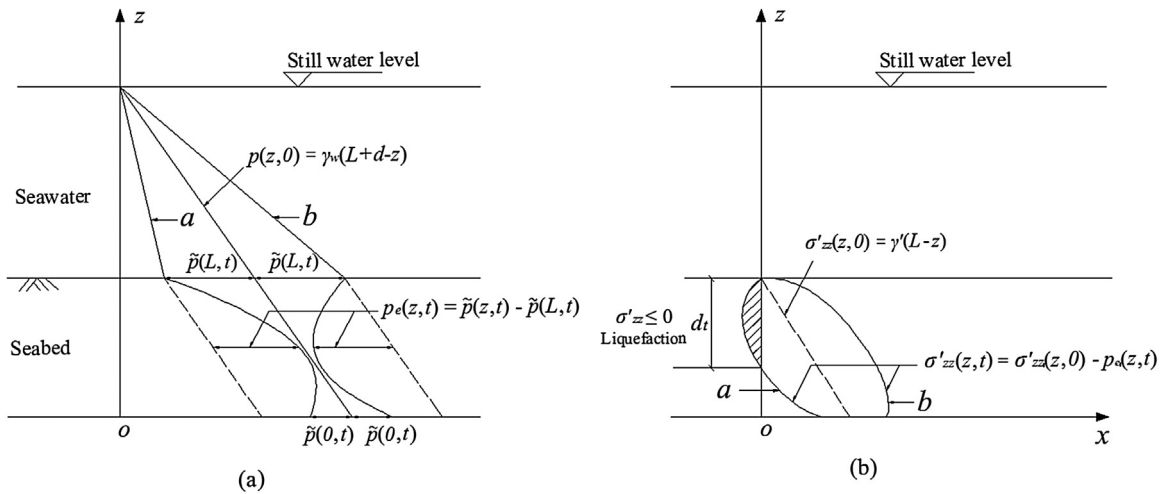


Fig. 6. Concept of excess pore pressure and momentary liquefaction for vertical seismic excitation: (a) distribution of (pore) water pressure; (b) distribution of effective vertical stress.

sure change in the seabed under the action of earthquake peaks, depicted by the difference between the hydrostatic pressure line and dash lines in Fig. 6(a). The dash lines in Fig. 6(a) depict the distributions of hydrostatic pressures when the seabed surface is under the induced pressures of seawater. In addition, since the excess pore pressure is transient in nature, the effective stress also varies in accordance with the change of the excess pore pressure in the seabed. Zen and Yamazaki [9] have shown that the magnitude of the change in vertical effective stress is identical with the induced excess pore pressure in the seabed. And it has been conceived that the soil will be liquefied when the vertical effective stress instantaneous vanishes, thus losing its strength to bear any load, and consequently causing seabed instability. As depicted in Fig. 6(b), the criterion for the earthquake-induced liquefaction can be described as

$$\gamma'(L-z) - [\tilde{p}(z,t) - \tilde{p}(L,t)] \leq 0 \quad (27)$$

where γ' denotes the effective unit weight of soil. This inequality implies that liquefaction in a seabed may occur if the induced excess pore pressure becomes greater than the overburden soil pressure. The liquefaction criterion employing the excess pore pressure in Eq. (27) could be an applicable means [6]. Consequently, the potential depth range of momentarily liquefied area in Fig. 6(b) is $d_t \leq z \leq L$.

4.2. Depth of liquefied seabed area

The analytical solutions for the vertically earthquake-induced response, which are given in Section 1, contain three main groups of parameters as follows: seawater parameters such as water depth d ; seabed parameters including seabed thickness L , hydraulic permeability k_f , porosity n , Poisson's ratio ν , saturation degree S_r , fluid compressibility β , shear modulus μ ; and earthquake ground motion parameters represented by excitation frequency f and displacement amplitude u_0 . In these parameters, the fluid compressibility β depends on the water depth d and saturation degree S_r , as illustrated in Fig. 5. The effects of permeability k_f can be considered as a main factor to distinguish different marine soil types. In the following parametric analysis, the porosity n and Poisson's ratio ν of the marine soils are assumed to be constants and the degree of saturation is considered to vary from 99% to 100%.

The seawater depth does not only influence the pore fluid compressibility β through Eq. (5) but also determines the dynamic seawater pressure on the seabed surface as described in Eq. (20). Therefore, the depth of the seawater above the seabed is a domi-

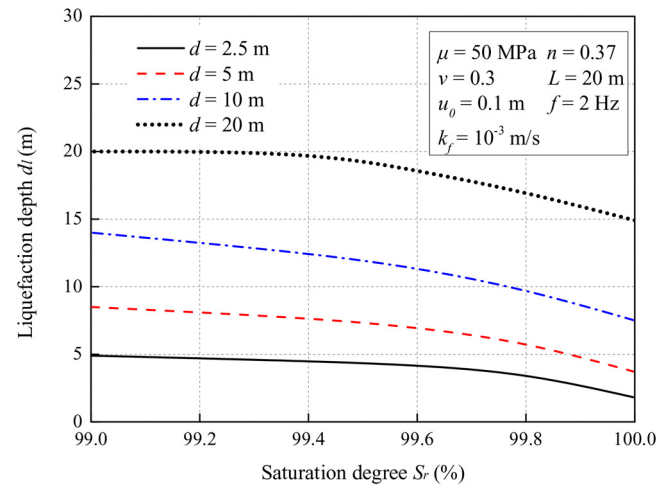


Fig. 7. Variation of liquefaction depth d_t with saturation degree S_r for different water depths.

nant factor for the seismically induced response of porous seabed. Fig. 7 depicts the influence of seawater depth on the variation of liquefaction depth with saturation degree. The depths of seawater are selected to be 2.5 m, 5 m, 10 m and 20 m, respectively. It is shown that the liquefaction depth decreases with the increasing of saturation degree in the nearly saturated seabed. This is due to the fact that the induced pore pressure will increase when the saturation degree approaches fully saturated state, which are explained in Eq. (25) and Fig. 5. As shown in Fig. 7, the liquefaction depth also increases with the depth of seawater. This is because the dynamic water pressure at the surface of seabed is proportionate to the water depth. Moreover, in the case of complete saturation, the depth of liquefied area is found to be in proportion to the water depth.

Fig. 8 shows the influence of seabed thickness on the variation of liquefaction depth with saturation degree. The liquefaction depth increases with the thickness of seabed when the porous seabed is not completely saturated. However, it should be noted that the depth of liquefied area almost remains constant (about 7.5m) when the seabed is fully saturated. Thus the liquefaction depth of saturated porous seabed is independent of seabed thickness.

In Fig. 9, the influence of soil permeability on the liquefaction depth is insignificant. Because larger pore pressure will be generated in the earthquake with higher frequency or larger exci-

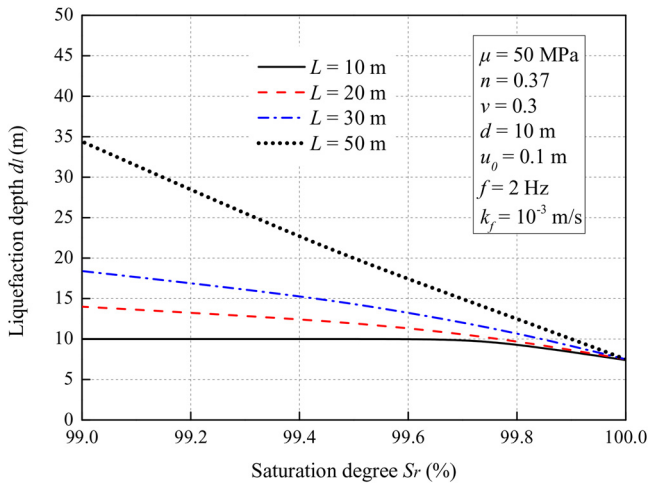


Fig. 8. Variation of liquefaction depth d_l with saturation degree S_r for different seabed thicknesses.

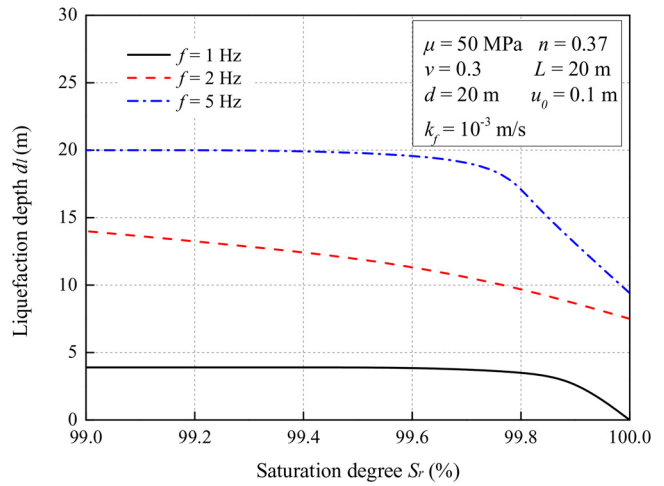


Fig. 10. Variation of liquefaction depth d_l with saturation degree S_r for different earthquake frequencies.

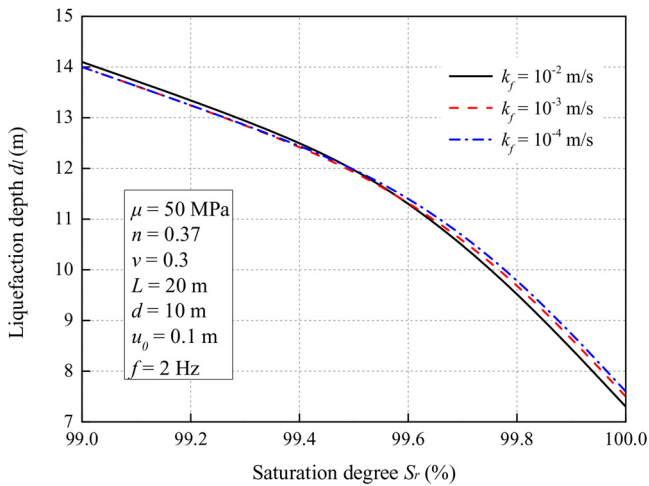


Fig. 9. Variation of liquefaction depth d_l with saturation degree S_r for different soil permeabilities.

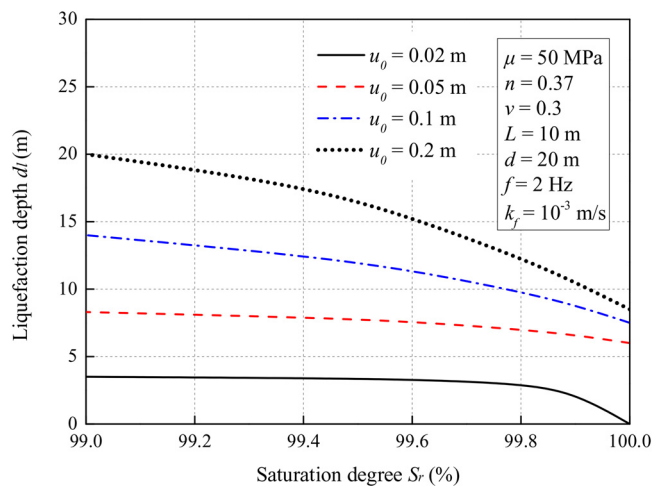


Fig. 11. Variation of liquefaction depth d_l with saturation degree S_r for different excitation displacement amplitudes.

tation displacement, the liquefaction depth also increases with the earthquake frequency and displacement amplitude, as shown in Figs. 10 and 11. The shear modulus also has marked effect on the liquefaction of the cohesionless soil seabed. As illustrated in Fig. 12, the liquefaction depth increases with the shear modulus when the porous seabed is not completely saturated. However, it is worthwhile to note that the depth of liquefied area remains at about 7.5 m when the seabed is fully saturated.

5. Conclusions

The aim of this paper is to analyze the momentary liquefaction phenomenon of porous seabed under the action of vertical earthquake, which has traditionally been ignored in geotechnical earthquake engineering. It should be noted that the momentary mechanism discussed here adopts poro-elastic theory, which is different from the residual one based on elasto-plastic analysis. Therefore, the conclusions drawn in this paper are limited to the momentary liquefaction instead of the residual one caused by the build-up of pore pressure under cyclic shearing. The analytical solutions of the induced displacements and pore pressure are mathematically derived as a function of seawater depth, soil properties, seabed thickness, excitation frequency and amplitude. The significant finding is that current understanding that the vertical motion

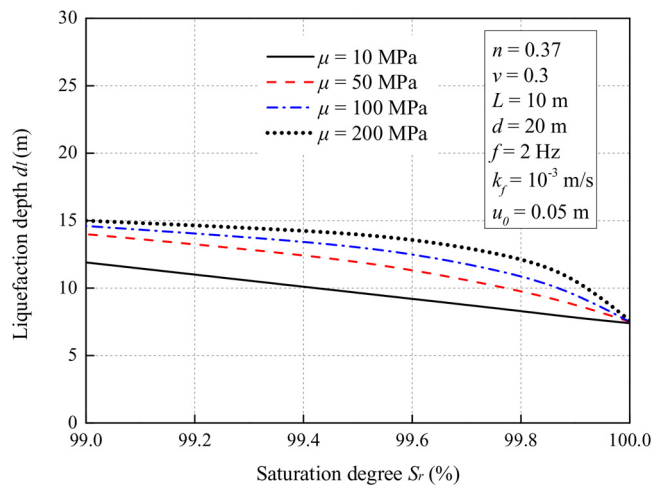


Fig. 12. Variation of liquefaction depth d_l with saturation degree S_r for different shear moduli.

effect on soil liquefaction is negligible may not always hold true and the following conclusions could be summarized:

- (1) Even if the degree of saturation is only slightly below full saturation, its impact on the seismically induced response such as displacement and pore pressure is significant.
- (2) The earthquake-induced pore pressure in the seabed reaches the maximum near the middle position.
- (3) Based on the proposed criterion for the momentary earthquake liquefaction in the seabed, the liquefaction of the cohesionless soil seabed happens from the seabed surface.
- (4) The liquefaction of seabed is influenced by seawater parameters, seabed parameters and earthquake ground motion parameters.
- (5) The saturation degree of soil, earthquake frequency and displacement amplitude of excitation are major influencing factors determining the depth of liquefied seabed.
- (6) When the seabed is fully saturated, the liquefaction depth of seabed is found to be proportionate to seawater depth while independent of seabed thicknesses and shear modulus.
- (7) The liquefaction occurs from the shallow layer of seabed where most of construction of marine structures are installed, which should merit our attention in practical engineering.

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